Cycloidal Displacement

The equation of cycloidal displacement, as shown in Fig 1, is:

$$s = h \left[\frac{\theta}{\beta} - \frac{1}{2\pi} \sin\left(2\pi \frac{\theta}{\beta}\right) \right]$$

The displacement s is the projection of a point of cycloidal curve, which is generated by rolling a circle on a line, to the s-axis (y-axis).

The velocity, acceleration and jerk equations are:

$$v = \frac{h}{\beta} \left[1 - \cos\left(2\pi \frac{\theta}{\beta}\right) \right]$$
$$a = 2\pi \frac{h}{\beta^2} \sin\left(2\pi \frac{\theta}{\beta}\right)$$
$$j = 4\pi^2 \frac{h}{\beta^3} \sin\left(2\pi \frac{\theta}{\beta}\right)$$

where h is the total rise, or lift, θ is the camshaft angle, and β is the total angle of the rise interval. The s v a j diagrams are shown in Fig. 2.

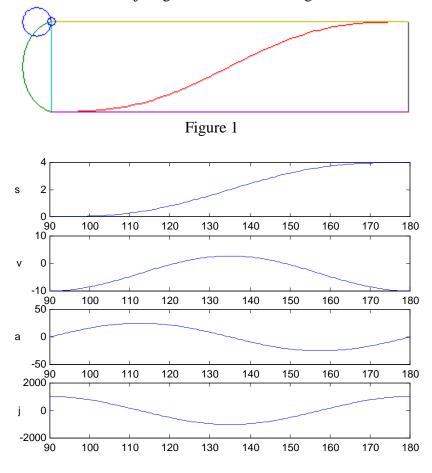


Figure 2