# LINEAR CIRCUITS ANALYSIS & SYNTHESIS

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# A note to the reader

In this PDF file, you'll find hints and answers to select end-chapter problems of the text Linear Circuits: Analysis & Synthesis by A. Ramakalyan OUP India, 2004, ISBN: 0-19-567001-9 Please send an email to the author: rkalyn @ nitt.edu

with your feedback as well as queries

- 1. The battery releases energy;  $E = 1.5 \times \text{charge of an electron.}$
- 2.  $v_{max} = 5\sqrt{5} \text{ V}$ , and  $i_{max} = 1/(40\sqrt{5}) \text{ A}$
- 3. 48.4 kW
- 4. 0.2W, 20V
- 5.  $v_s = 10.2$  V, and  $r = 2\Omega$
- 6. 300  $\Omega$ , 0.4833  $\mp$  0.05 A
- 7.  $6 \times 360 \times 9$  J,  $6 \times 360$  C
- 8. Rs. 82.80
- 9. 101.25 J absorbed
- 10. releases
- 11.  $Q = \int_{t_1}^{t_2} i(t)dt$ , and  $W = Q \int_{t_1}^{t_2} v(t)dt$
- 12. A current of 3A flows in the counterclockwise direction in the mesh.
- 13. A current of 3A flows in the clockwise direction in the mesh.
- 14. Element X absorbs 6W and the 2A source absorbs 4W.
- 15. The 5A source releases 25W, and the element X absorbs 15W.
- 16. The current source releases energy.
- 17. Working is similar to that of problem 2.16.
- 18. Assume that the internal resistance r is in  $\Omega$ . Use the following equations:

$$
i_s = 11.965 + \frac{119.65}{r}
$$
  

$$
i_s = 11.695 + 116.95 \left(\frac{1}{r} + \frac{1}{1000}\right)
$$

- 19. You will get a pair of equations similar to those of problem 2.18.
- 20. The bulb is turned OFF if one of the two switches is in OFF position. If both the switches are either ON or OFF, then the bulb is turned ON.

- 1. All are networks; (a) is not a circuit.
- 2. 4 nodes, 3 meshes, and 7 loops.
- 3. Problems 3.3 to 3.9 may be done quite trivially.
- 10.  $1.5 k\Omega$ ; 10 mW (6 mW + 4 mW).
- 11. 12 $\Omega$ ; 1.25 (0.75 + 0.5) W.
- 12.  $0.2k$  Ω

13. 
$$
\frac{1}{12}k\Omega
$$

- 14. Yes; the current source delivers.
- 15.  $E_1$ ,  $E_3$ , and  $E_5$  are active elements.
- 16. This problem does not require any hint.
- 17. The circuit is inconsitent; it does not obey KCR.
- 18.  $E_2$ : 4V with positive potential to the left,  $E_3$ : 6V with the positive potential to the right, and  $E_4$ : 4V with the positive potential to the right.

19.

$$
[(30||10) + (5||5)] ||25 + 20
$$

20.

$$
[(3||18) + 10] || 6 || 30
$$

- 21. This problem does not require any hint.
- 22. The currents, in milli amperes, are as follows from left to right:

$$
\frac{1}{3},\,1,\,\frac{4}{3},\,\frac{8}{3},\,\frac{16}{3},\,\frac{14}{3}
$$

- 23. Use series-parallel reductions.
- 24. 60 21  $\Omega, \frac{45}{21}$ 21  $\Omega$ ,  $\frac{7}{5}$ 5  $\Omega$
- 25. This problem does not require any hint.
- 26. Follow the argument on ladder networks in the text.
- 27. Reduce this to a single series-parallel circuit.
- 28. The VCVS delivers power. Using nodal analysis you get the following equations:

$$
45 v_1 - 37 v_2 = 0
$$
  
-169 v<sub>1</sub> + 207 v<sub>2</sub> = 336

Using  $v_1$  and  $v_2$ , we get  $v_x = v_1 - v_2$ , and  $v_3 = v_1 - 6v_x$ . It is now easy to compute the current through the VCVS.

#### Chapter 4

In this chapter, there are typographical errors in problems 8 and 26.

1. Use the following linear system of equations:

$$
\frac{1}{15} \begin{bmatrix} 8 & -3 & 0 & 0 \\ -3 & 7.5 & -3 & 0 \\ 0 & -3 & 6 & -3 \\ 0 & 0 & -3 & 4.5 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \end{bmatrix} = \begin{bmatrix} 2 \\ 0 \\ -2 \\ 6 \end{bmatrix}
$$

1  $\overline{1}$  $\overline{1}$  $\overline{1}$  $\overline{1}$  $\perp$  $\overline{1}$  $\overline{1}$  $\overline{1}$  $\overline{1}$  2. Use the following equations:

$$
\frac{1}{60} \begin{bmatrix} 30 & -10 \\ -10 & 17 \end{bmatrix} \begin{bmatrix} v_2 \\ v_3 \end{bmatrix} = \begin{bmatrix} -16/3 \\ 5/24 \end{bmatrix}
$$

- 3. The current through  $4\Omega$  resistor is 15.365 A from bottom to top.
- 4. Enumerating the nodes in the counterclockwise direction with  $v_1$  at the apex,

$$
v_1 = \frac{125}{7}
$$
,  $v_2 = \frac{55}{7}$ ,  $v_3 = \frac{475}{7}$ , and  $v_4 = -5$  V

- 5. Mesh currents are already available; use mesh analysis.
- 6.  $i_1 = -4$  A,  $i_2 = 4$ A, and  $i_3 = 0$  A
- 7. You need to solve for only one mesh current.
- 8. There is a typographical error in this problem. The second voltage source at the extreme right should be 20V with the negative terminal at the top. There are several possible solutions satisfying

$$
R_1 + R_2 = 2.5 k\Omega
$$

- 9. Use repeated source transformation followed by mesh analysis.
- 10. Obtain the mesh equations, and look at the mesh incidence matrix  $\mathcal{M}$ . You will notice that

$$
v_1\,+\,v_2\,=\,v_3
$$

with  $v_1 \neq 0$ ,  $v_2 \neq 0$ , and  $v_3 \neq 0$  will solve the problem since KVR has to be obeyed by the loop comprising the three voltage sources.

- 11. 14 mW
- 12. 1/450 mW
- 13.  $21 \cdot v_4 = 10 \cdot i_A + 80 \cdot i_B$
- 14. The required number is 'n'.
- 15. Assume  $i_A$ ,  $i_B$ , and  $v_C$  arbitrarily and solve for  $\alpha$ ,  $\beta$ , and  $\gamma$  in the following:

$$
\begin{bmatrix}\ni_A & i_B & 0 \\
i_A & 0 & v_C \\
0 & i_B & v_C\n\end{bmatrix}\n\begin{bmatrix}\n\alpha \\
\beta \\
\gamma\n\end{bmatrix} =\n\begin{bmatrix}\n20 \\
-5 \\
2\n\end{bmatrix}
$$

16.  $R_{eq} = 14/3 k\Omega, v_{OC} = 5/3V$ 

- 17.  $R_{eq} = 0$
- 18.  $R_{eq} = 800/13 k\Omega, v_{OC} = 1160/13 V$ 19.

$$
v_{50} = \frac{50}{50 + 800/13} \cdot v_{OC} \text{ V}, \ \ P_{50} = v_{50}^2/50 \text{ W}
$$

- 20.  $R_L = 5/6 k\Omega$
- 21.  $r = 80\Omega = R_L$ ,  $v_S = 200V$ , and  $P_{max} = 125 W$
- 22. Find  $R_{eq}$  as seen by  $R_L$ .
- 23. Use the following equations:

$$
R_L = 2R + [R || (2R + R_s)]
$$
  

$$
R_s = 2R + [R || (2R + R_L)]
$$

24. Since  $P \propto i^2$ , take  $i \propto \pm \sqrt{P}$ . You get

$$
k = -\frac{24}{11}
$$
 or  $-\frac{40}{13}$ 

- 25. This problem may be solved triviallly.
- 26. There is a typographical error. The resistor above the controlled source should be 10 kΩ instead of 10Ω. Each of the independent sources delivers  $5/11$  mW, and the controlled source absorbs 50/121 mW.

27.  $i_x = 29$  A

28. Trivially, use a test voltage source  $v_{test}$  and compute the current it delivers.

29. Compute the equivalent resistance  $R_{eq}$  as seen by the port A-B;  $R_L = R_{eq}$ .

# Chapter 5

In this chapter, there are typographical errors in problems 4 and 16.

- 1.  $i_L(0^+) = 1$  A,  $i_L(\infty) = 0$ , and  $\tau = 10$  milliseconds.
- 2.  $i_L(0^+) = 5$  mA,  $i_L(\infty) = 0$ , and  $\tau = 1/15$  microseconds.  $y(0^+) = -150$ V, and  $y(\infty) = 0.$
- 3.  $y(0^+) = i_L(0^+) = 5/6$  mA,  $y(\infty) = 0$ , and  $\tau = 0.2$  microseconds.
- 4. There is a typographical error in the circuit. The controlled source is a CCVS with positive terminal at the top, and the proportionality constant is 8000 with the controlling variable  $i_s$ .  $v_C(0^+) = 0$ , and  $v_C(\infty) = 4V$  with the time constant  $\tau = 6$  milliseconds.
- 5.  $y(t) = 35 e^{-t/\tau}$  V, with  $\tau = 20$  microseconds.
- 6.  $\tau = 5$  seconds. Use nodal analysis for  $t < 0$  and for  $t \ge 0$  with the initial capacitor voltage.
- 7. Use a test voltage source  $v_{test}$  to compute the equivalent resistance as seen by the capacitor for  $t \geq 0$ .
- 8. This problem may also be solved using a  $v_{test}$  to compute the equivalent resistance, and then using nodal analysis.
- 9. Make necessary computations using nodal analysis for the following time intervals:

 $t < 2, 2 \leq t < 3, \text{ and } 3 \leq t \leq \infty$ 

Alternatively, you may use the property of time-invariance.

10. First compute the common node potential for both the inductors. It turns out to be

$$
v_L(t) \, = \, \frac{20}{3} \, e^{-t/\tau}
$$

Use this inductor voltage to compute the current.

- 11. Use nodal analysis. Also use a test voltage source  $v_{test}$  to compute the  $R_{eq}$ .
- 12. Use nodal analysis. Remember that the series combination of two equal capacitances is just half of the individual capacitances.
- 13. This problem requires a careful computation of the initial conditions at the time of switching.

$$
v_C(0^+) = 2 \text{ V}
$$
  
\n
$$
\tau_1 = 12 \text{ millisec}
$$
  
\n
$$
v_C^1(t) = 6 - 4e^{-t/\tau_1}
$$
  
\n
$$
\Rightarrow v_C(1^+ \text{ millisec}) = 6 - 4e^{-1/12}
$$
  
\n
$$
\tau_2 = 10 \text{ millisec}
$$
  
\n
$$
\vdots
$$

14. The differential equation is

$$
\frac{d^2}{dt^2}v_C(t) + 10^4 \frac{d}{dt}v_C(t) + 5 \times 10^8 v_C(t) = -5 \times 10^9
$$

- 15. Neglect the initial conditions.
- 16. There is a typographical error in the circuit. Across the  $50 \Omega$  resistor, the voltage  $v_x$  is defined with the positive polarity at the bottom. You'll get the following differential equation:

$$
\frac{d^2}{dt^2} y(t) + \frac{1}{300C} \frac{d}{dt} y(t) + \frac{1}{LC} y(t) = 0
$$

- 17. Look at the differential equation for the above problem.
- 18. Apply nodal analysis and make use of the appropriate initial conditions.
- 19. This problem does not require any hint.
- 20. Observe that this is a parallel RLC circuit for  $t \geq 0$ .
- 21. Obtain the step response and use the time-invariance property.
- 22. Use nodal analysis.
- 23. This problem does not require any hint.
- 24. Solve for  $i_L(t)$  using the following differential equation:

$$
\frac{d^2}{dt^2} i_L(t) + \frac{R}{L} \frac{d}{dt} i_L(t) + \frac{1}{LC} i_L(t) = \frac{1}{LC}
$$

with the initial conditions:

$$
i_L(0^+) = 0
$$
 and  $\frac{d}{dt}i_L(t)|_{t=0^+} = -20000$ 

Then solve for  $y(t)$  using:

$$
y(t) = L\frac{d}{dt}i_L + R \cdot i_L
$$

- 25. This problem does not require any hint.
- 26. This problem does not require any hint.
- 27. This problem does not require any hint.
- 28. This problem does not require any hint.
- 29. Use the following differential equation:

$$
\ddot{y} + 3000 \dot{y} + 5 \times 10^8 y = 3 \times 10^9 \quad \forall t \ge 0
$$

30. Use nodal analysis.

1. The differential equation is

$$
RC\,\frac{dv_C}{dt} + v_C = R \cdot i_S
$$

- 2.  $v_R = 2\angle 0^\circ 2$ √  $\overline{2}$ ∠ – 60<sup>o</sup>
- 3. (a)  $1.064 \Omega$
- 4.  $\omega = 2000$ ,  $j\omega L = j20$ , and

$$
i_R = \frac{j20}{10 + j20} 6\angle 0^o
$$
 and  $v_R = 10 \cdot i_R$ 

- 5. With  $\omega = 120\pi$ , replace L and C with their respective reactances and use mesh analysis.
- 6. With the given  $\omega$ , use appropriate reactances:

$$
\mathcal{Z} = (j\omega L) \parallel \left(\frac{1}{j\omega C}\right)
$$

7.

$$
\mathcal{Z} = \left(\frac{1}{j\omega C}\right) + \left(R \,\|\, j\omega L\right)
$$

- 8. This problem does not require any hint.
- 9. Use  $\omega = 1000$
- 10. Use  $\omega = 10000$
- 11. Use complex numbers. You get the following LSE:

$$
\begin{bmatrix} -j0.02 & +j0.02 \\ +j0.02 & 0.04 + j0.08 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \end{bmatrix} = \begin{bmatrix} 10\angle 30^\circ \\ 0 \end{bmatrix}
$$

12. This problem does not require any hint.

- 13. Use nodal analysis.
- 14. This problem does not require any hint.
- 15. Use  $v_S = 10$  and  $i_S = -j50$ .
- 16. This problem does not require any hint.
- 17. This problem does not require any hint.
- 18.  $v_1 = 10 j20$  V
- 19. Use mesh/nodal analysis.
- 20. This problem does not require any hint.
- 21. Use complex algebra and solve the following LSE:

$$
\frac{v_{oc} - 10\angle 45^o}{j2} + \frac{v_{oc}}{-j10} = 0
$$
  

$$
\frac{10\angle 45^o}{5} + \frac{10\angle 45^o - v_{oc}}{j2} = 0
$$

- 22. This problem does not require any hint.
- 23. This problem does not require any hint.
- 24. Use  $\omega = 10^4$  rad/sec, and replace L and C with their respective reactances.
- 25. Use mesh analysis.
- 26. Solve for  $v_{Th}$  and  $\mathcal{Z}_{Th}$  in the following pair of equations:

$$
\frac{1000}{\mathcal{Z}_{Th} + 1000} \cdot v_{Th} = 2\angle -30^{\circ}
$$

$$
-j1000
$$

$$
\frac{-j1000}{\mathcal{Z}_{Th} - j1000} \cdot v_{Th} = 3\angle -135^{\circ}
$$

- 27.  $R_1 \times R_2 \times C = L$
- 28. This problem does not require any hint.

29. Define

$$
\mathcal{Z}_1 \ \stackrel{\Delta}{=} \ \frac{R_1}{1 + j\omega R_1 C_1}
$$

Use this  $\mathcal{Z}_1$  in the following equation:

$$
\frac{R_2}{R_2 + \mathcal{Z}_1} = \frac{R_L + j\omega L_L}{R_L + R_3 + j\omega L_L}
$$

30. Define

$$
\mathcal{Z}_1 \triangleq R_1 + \frac{1}{j\omega C_1}
$$

and use this definition as in the above problem.

# Chapter 7

1. It is easy to verify that for  $\omega = 1$  rad/sec,

$$
H(j\omega) = \frac{1 - j2}{13 - j2} \times \frac{2}{2 + j1}
$$

- 2. Use complex algebra followed by voltage/current division rule.
- 3. Use nodal analysis and get the following pair of equations:

$$
\frac{v_1 - v_S}{2} + \frac{v_1}{2/j\omega} + \frac{v_1 - v_R}{j\omega/2} = 0
$$
  

$$
\frac{v_R - v_1}{j\omega/2} + \frac{v_R}{5/j\omega} + \frac{v_R}{5} = 0
$$

- 4. Use mesh analysis.
- 5. Use mesh analysis.
- 6. Use mesh analysis.

7.

$$
\mathcal{Z}_{series} = 1000 + j \left( 0.01\omega - \frac{10^9}{\omega} \right) \Omega
$$

$$
\mathcal{Y}_{parallel} = \frac{1}{1000} + j \left( 10^{-9}\omega - \frac{100}{\omega} \right) \Omega^{-1}
$$

8.  $\omega = 0$  is the frequency when the magnitude is unity. For obtaining maximum magnitude and the frequency at which the magnitude attains maximum, use

$$
\zeta = 0.2 \text{ and } \omega_n = 50
$$

9. Rewrite the transfer function as:

$$
H(j\omega) = \left(1 + \frac{j\omega}{10}\right) \cdot \frac{1}{\left(1 + \frac{j\omega}{100}\right)}
$$

10. Rewrite the transfer function as:

$$
H(j\omega) = \frac{1}{(j\omega)^2} \cdot \left(1 + \frac{j\omega}{10}\right)^2 \cdot \frac{1}{\left(1 + \frac{j\omega}{10^4}\right)} \cdot 10^4
$$

11. Rewrite the transfer function as:

$$
H(j\omega) = (1 + j\omega) \cdot \frac{1}{\left(1 + \frac{j\omega}{10}\right)} \cdot \frac{1}{\left(1 + \frac{j\omega}{100}\right)}
$$

- 12. There are two different second-order factors. Compute  $\zeta$  and  $\omega_n$  for each of the factors carefully.
- 13. Resonance.
- 14.  $\omega = 1$  Mrad/sec.
- 15. Use standard formulae relating Q, half-power frequencies, and the bandwidth.
- 16. In this problem,  $R_{eff} = 25 + R + 10 \Omega$ . Given L and  $\omega_n = 1/$ √  $LC$ , you may quickly compute C. Thereafter use standard formulae as in the above problem.
- 17. If you use source transformation, you would immediately get a parallel RLC circuit. Use standard formulae.
- 18. In this case,  $R_{eff} = R||R_s$ .
- 19. This problem does not require any hint.
- 20. This problem does not require any hint.
- 21. Use the definition of  $Q$  in terms of energy dissipation.
- 22. Find the resonant frequency.
- 23. Find the resonant frequency.

- 1. Use phasors to compute the required voltages and currents. Express them in the trigonometric form, with magnitude, frequency, and the phase angle. Obtain the  $v(t) \cdot i(t)$  products.
- 2. Use mesh analysis.
- 3. Use mesh analysis.
- 4. Use mesh analysis.
- 5. Compute the Thévenin's equivalent.
- 6. Compute the Thévenin's equivalent.
- 7. Look at the magnitude part.
- 8. Recall that the frequency of  $p(t)$  is twice that of  $v(t)$ . Accordingly,  $\omega = 1000\pi$ rad/sec. Thereafter, use standard formulae.
- 9. Find the admittance  $\mathcal{Y}_{eq}$  as seen by the source.
- 10. Use the relationship:

$$
\frac{Q}{P} = \tan \phi = \frac{X}{R}
$$

- 11. Follow example 8.6.
- 12. Follow example 8.6.
- 13. Use KVR and compute  $v_s$  and  $i_s$ .  $S = \mathcal{V} \cdot \mathcal{I}^*$ .
- 14. Follow example 8.6.
- 15. This problem does not require any hint.
- 16. Use standard formulae.
- 17. Use star delta transformation.
- 18. Use per-phase analysis.
- 19. Use per-phase analysis.
- 20. Use per-phase analysis.
- 21. Use per-phase analysis.
- 22. Use delta star transformation at the load end. Perform per-phase analysis. On these results make appropriate line - phase transformations.
- 23. Use delta star transformation at the load end. Perform per-phase analysis. On these results make appropriate line - phase transformations.
- 24. This problem does not require any hint.
- 25. Use standard formulae.
- 26. This problem does not require any hint.
- 27. Use per-phase analysis.
- 28. Use per-phase analysis.
- 29. Follow examples 8.17 and 8.18.
- 30. Use standard relationships and perform per-phase analysis.

2.

#### In this chapter, there are typographical errors in problems 1, 28, and 30.

- 1. There are a few typographical errors in this problem. Sub-problem numbers (i), (iii), (v), and (vii) are missing. In the sub-problem (vii), the phasor should be  $\mathcal{I} = 10\angle 0^o.$ 
	- $(i) s = 0$  $(ii) s = -0.1$ (iii)  $s = -5 + j100$  $(iv) s = j100$ (v)  $s = -5.1 + j8.6, 10\angle{60^{\circ}} = 10e^{-5.1t}\cos(8.6t + 60^{\circ})$ (vi)  $10\angle -45^{\circ} = 10e^{-5.1t}\cos(8.6t - 45^{\circ})$ (vii)  $10\angle 0^{\circ} = 10$  A, dc (viii)  $10 \cos(10^6 t)$

$$
\frac{1}{2} \cdot \frac{s\mathcal{V}_s(s)}{s^2 + 2.5s + 5}
$$

3. The transfer function may be written as:

$$
\frac{Y(s)}{U(s)} = \frac{s+4}{s(s+1)(s+1+5)(s+1-j5)}
$$

Cross-multiply to get the required differential equation.

- 4. Similar to problem 9.3.
- 5. The transfer functions are

$$
10 \frac{(s+1)(s+6)}{s(s+5)^2(s+7)}
$$
 and 
$$
\frac{s(s^2+10s+50)}{(s^2+4)(s^2+6s+10)}
$$

6.

$$
\frac{10^6/5s}{100+0.01s+10^6/5s} \cdot (10+0.01s)
$$

7. Replace  $L$  and  $C$  with  $sL$  and  $1/sC$  respectively, and use algebra. 8.  $e^{-10^5t}$  V 9.

$$
\dot{v}_C = -10^4 v_C + 5 \times 10^3 v_i
$$

- 10. Use mesh analysis.
- 11. Use mesh analysis.
- 12. Use mesh analysis.

13. Use the properties of Laplace transformation.

14. Express  $f(t)$  as a sum of appropriate ramp functions.

15. 
$$
f(t) = 2e^{-t} - e^{-3t}
$$
  
16.

$$
F(s) = 6 \cdot \frac{s^2 + 5}{(s + j1)(s - j1)(s + j2)(s - j2)}
$$

17.

$$
\frac{(s+3)y(0) + \dot{y}(0)}{\underbrace{(s+1)(s+2)}} + \frac{2s/(s^2+4)}{\underbrace{(s+1)(s+2)}}\
$$

- 18. First obtain the ODE.
- 19. Unit step function is the integral of unit impulse function.
- 20. Assume that we are interested in  $t \geq 0$ . Both the sources are  $5/s$ ,  $R = 1 k\Omega$ , and  $C = 10^6/s.$
- 21.  $L = 0.001s$ .
- 22.  $v_S(s) = 10s/(s^2 + 10^{12})$ . Use mesh analysis.
- 23. Use mesh analysis.
- 24. Use nodal analysis.  $v_S(s) = 10/s^2$
- 25. Use the initial conditions with  $v_S(s) = 1/s$ .
- 26. This problem does not require any hint.
- 27.  $v_S(t) = 10 5q(t)$ . Use the initial conditions.
- 28. There is a typographical error in this problem. It should be read as  $i_S = 2e^{-t}$  mA for  $t \geq 0$ .  $i_S(s) = 2/(s + 1)$ . Use initial conditions.
- 29. Similar to the above problem.
- 30. There is a typographical error in the figure. The output  $v_0(t)$  should be across the 10 kΩ resistor at the extreme right. First obtain the transfer function  $H(s)$ . Express  $v<sub>S</sub>(t)$  in terms of its Laplace transform. Use the property that convolution in time is multiplication is s-domain.

- 1. The series elements are  $1 \mp j1 \Omega$ , and the shunt element is  $1 \Omega$ .
- 2. This problem does not require any hint.
- 3. Use star delta transformation.
- 4. Similar to problem 10.1.
- 5. This problem does not require any hint.

6. Take care of the VCVS while computing  $z_{21}$  and  $z_{22}$ . The matrix is

$$
\left[\begin{array}{cc} 3R & 2R \\ 2R(k+1) & 2R(k+1) \end{array}\right]
$$

- 7. Obtain the Y parameters, and then the Z parameters. Or, equivalently, use delta - star conversion.
- 8. From the standard definitions, identify appropriate parameters, and use the relationship among the parameters.
- 9. Follow the definitions.
- 10. Similar to problem 10.8.
- 11. Follow the definitions.
- 12. Follow the definitions.
- 13. Follow the definitions.
- 14. Follow the definitions. Also, use the relationship between h and T parameters.
- 15. Similar to problem 10.8.
- 16. Follow the definitions, and use the relationship among the parameters.
- 17. First obtain the elements of the network, and then proceed as per the instructions given in the problem.
- 18. Follow the equations given in section 10.4.1 on amplifiers.
- 19. Similar to problem 10.17.
- 20. Follow the definitions. Also, look at the circuit as an appropriate "interconnection" of two T-networks.
- 21. Follow the definitions. Also, look at the circuit as an appropriate "interconnection" of two T-networks.
- 22. See the network as a cascade connection.
- 23. Use T parameters on the cascade.
- 24. Obtain the network elements and proceed as per the instructions given in the problem.
- 25.  $z_{11} = v_1/i_1$  with  $i_2 = 0$ .
- 26.  $z_{11} = v_1/i_1$  with  $i_2 = 0$ , and  $y_{11} = i_1/v_1$  with  $v_2 = 0$ .
- 27. Use a continued fraction similar to what you have done for the ladder networks in chapter 3.
- 28. This problem does not require any hint.
- 29. A simple series network!
- 30. Use a continued fraction.

#### In this chapter, there is a typographical error in problem 10.

- 1. Simple linear equations.  $a_4 = +1$ ,  $a_2 = -1$ , and  $a_0 = +1$ .
- 2. Graphical calculation.
- 3. Graphical calculation.
- 4. Verify as instructed in the problem.
- 5. This problem does not require any hint.
- 6. Make the circuit as per the directions given in the problem and apply nodal analysis.
- 7.  $Y(s) = N(s)/D(s)$  with  $deg[N(s)] > deg[D(s)] + 1$ .
- 8.  $\alpha$  is a negative real number.
- 9. Assume arbitrary functions, and verify the properties.
- 10. There is a typographical error in part (d) of this problem. In the numerator the second term should be  $6s^2$ . Look at the zero-pole location.
- 11. Follow the hint given at the end of the problem, and solve for the constants using the given data.
- 12. Use the properties of pr functions.
- 13. Locate the zeros and the poles in terms of the coefficients of the polynomials.
- 14. Obtain the driving point impedance of the given network and compare it with

$$
\frac{(s+2)(s+4)}{(s+1)(s+3)}
$$

- 15. This problem does not require any hint. For Foster II form, remember to expand  $Y(s)/s$  as a sum of partial fractions.
- 16. Similar to problem 11.15.
- 17. Expand  $Z(s)$  as a continued fraction. Remember not to expand  $1/Z(s)!$
- 18. Use Cauer forms. Put the continued fraction and examine the resulting  $Z(s)$ .
- 19. The driving point impedance is

$$
z_{11}(s) = \frac{75}{3} \frac{(s+2)(s+4)}{(s+1)(s+3)}
$$

- 20. This problem does not require any hint.
- 21. Obtain the impedance function and examine the numerator and denominator polynomials.
- 22. This problem does not require any hint.
- 23. This problem does not require any hint.
- 24. This problem does not require any hint.
- 25. Obtain  $Z(s)$  and use this to synthesize Foster and Cauer forms.
- 26. Make a Cauer network, obtain its driving point function, and study the numerator and denominator polynomials.
- 27. Instructions are given in the problem itself.
- 28. Look at the hint for problem 11.26.
- 29. Use scaling. Choose, for instance, the network with lower values of inductances.
- 30. Use scaling.

- 1. Use nodal analysis with the Op Amp rule:  $v_n = v_p$ .
- 2. Similar to problem 12.1.
- 3. Similar to problem 12.1.
- 4. Similar to problem 12.1.
- 5. Similar to problem 12.1.
- 6. Similar to problem 12.1.
- 7. Similar to problem 12.1.
- 8. Obtain the transfer function  $H(s)$  and use Laplace transformation.
- 10. Use Laplace transformation.
- 12. Use Laplace transformation, and take care of the initial condition.
- 14. Use transient analysis. cf. Chapter 5.
- 15. Use Laplace transformation and the property of time-invariance.
- 16. Use transient analysis.
- 19. Obtain  $Z_i(s)$  and put it in the form of  $s \cdot (.)$ .
- 20. Use phasors and replace  $C$  with its reactance.
- 22. A band pass filter should have an initial attenuation, followed by a mid-band gain, and then followed by an attenuation at higher frequencies.
- 23. Obtain the ordinary differential equation using nodal analysis.
- 25. Use s-domain analysis.
- 26. Use transient analysis.
- 27. Use transient analysis.
- 28. Use phasors.
- 29. Use phasors.
- 30. Use s-domain analysis.

- 1. Use standard formulae.
- 2. Use standard formulae.
- 3. Use standard formulae.
- 4. Use standard formulae.
- 5. Use standard formulae.
- 6. Use standard formulae. Notice the exponential while performing integration.
- 8. Use Parseval's formula.
- 11. Obtain the transfer function using phasors and use the properties of linearity and time-invariance.
- 12. Similar to problem 13.11.
- 14. Similar to problem 13.11.
- 15. Similar to problem 13.11.
- 18. Use Parseval's theorem.
- 19. Similar to problem 13.11.
- 20. Obtain the transfer function of the network, and use the properties of Fourier transform; particularly regarding convolution.
- 21. Obtain the transfer function of the network:  $sRC/(sRC + 1)$ .
- 22. Use Parseval's theorem.
- 24. Use phasors.